Introduction to Supervised Learning

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August 28, 2020

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2 ML Terminologies

- In ML Applications Examples
- 4 K-nearest Neighbours

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Outline



2 ML Terminologies

- 3 ML Applications Examples
- 4 K-nearest Neighbours

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So What is Machine Learning?

- Automating automation
- Getting computers to program themselves
- Writing software is the bottleneck
- Let the data do the work instead!





WHAT IS MACHINE LEARNING?

Machine learning allows computers to learn and infer from data.



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Machine Learning Problem Types

Based on Type of Data

• Supervised, Unsupervised, Semi supervised, Reinforcement Learning

• Based on Type of Output

• Regression, Classification

Based on Type of Model

• Generative, Discriminative

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Types of Learning based on Type of Data

Supervised learning

- Training data includes desired outputs.
- Trying to learn a relation between input data and the output
- Unsupervised learning
 - Training data does not include desired outputs.
 - Trying to understand the data.
- Semi supervised learning
 - Training data includes a few desired outputs.
- Reinforcement learning
 - Rewards from sequence of actions.

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SUPERVISED LEARNING OVERVIEW



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Types of Learning based on Type of Output

Regression

A regression model predicts continuous values.

For example:

- What is the value of a house in California?
- What is the probability that a user will click on this ad?

Classification

A classification model predicts discrete values.

For example:

- Is a given email message spam or not spam?
- Is this an image of a dog, a cat, or a hamster?

Regression vs Classification

Classification (supervised learning)



Regression (supervised learning)



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REGRESSION: NUMERICAL ANSWERS



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CLASSIFICATION: CATEGORICAL ANSWERS



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CLASSIFICATION: CATEGORICAL ANSWERS



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Types of Learning based on Type of Model

Generative Model

A Generative nodel explicitly learns the actual distribution of each class.

Discriminative Model

A Discriminative model learns the decision boundary between the classes.

Generative Models

- Nave Bayes
- Hidden Markov Models
- Bayesian networks
- Markov random fields

Discriminative Models

- Logistic regression
- SVMs
- Traditional neural networks
- Nearest neighbor
- Conditional Random Fields (CRF)

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August 28, 2020

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Outline



2 ML Terminologies

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ML Basic Terminologies

Many terminologies associated with ML. Will cover them in the following slides.

- Labels
- Features
- Examples
- Models

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Label

- A label is the thing that we are predicting in classification or regression task. **Example:** Male, Female
- The label could also be the future price of wheat, the kind of animal shown in a picture, the meaning of an audio clip, or just about anything.
- Usually denoted with the variable y.

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Features (1/2)

- A feature is an input variable (a.k.a attribute).
- A simple machine learning project might use a single feature, while a more sophisticated machine learning project could use millions of features.
- Usually denoted as:

 $x_1, x_2, ..., x_N$

In the spam detector example, the features could include the following:

- words in the email text
- sender's address
- time of day the email was sent

• ...

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Features (2/2)

Generally three types of attributes:

- Categorical: red, blue, brown, yellow
- Ordinal: poor, satisfactory, good, excellent
- Numeric: 3.14, 6E23, 0,

Categorical

- No natural ordering to categories
- Categories usually encoded as numbers

Ordinal

- There is a natural ordering to categories
- Encoded as numbers to preserve ordering

Numeric

- Integers or real numbers
- meaningful to add, mul tiply, compute

Notethat

The process of generating this features for our machine learning problem is called feature engineering.

Data samples (Examples)

Data sample / Example is a particular instance of data, \mathbf{x} . (Note That. \mathbf{x} is a vector of features)

We break examples into two categories:

- Labeled examples: (Used for prediction)
- Unlabeled examples: (Used for inference/testing)

Example

housingMedianAge (feature)	totalRooms (feature)	totalBedrooms (feature)	medianHouseValue (label)
15	5612	1283	66900
19	7650	1901	80100
17	720	174	85700
14	1501	337	73400
20	1454	326	65500

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Model

A model defines a relationship between features and label.

Two phases of a model's life:

- **Training** means creating or learning the model. You show the model labeled examples and enable the model to gradually learn the relationships between features and label.
- **Testing/Inference** means applying the trained model to unlabeled examples. You use the trained model to make useful predictions (y').

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Outline



ML Terminologies





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ML Application 1: Credit Approval

Numeric Features:

- loan amount (e. g. \$1000)
- Income (e. g. \$65000)
- Ordinal Features:
 - savings: {none, <100, 100..500, 500..1000, >1000}
 - employed: {unemployed, <1yr, 1..4yrs, 4..7yrs, >7yrs}

• Categorical Features:

- purpose: {car, appliance, repairs, education, business}
- personal: {single, married, divorced, separated}

• Labels (Categorical):

- Approve credit application
- Disapprove credit application

Easy feature engineering process.

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ML Application 2: Handwritten Digits Recognation

Represent each pixel as a separate attribute either Categorical **OR** Ordinal:

- Categorical Features:
 - (white) or (black) based on a threshold
- Ordinal Features:
 - Degree of "blackness" of a pixel
- Labels (Categorical): {0,1,2,3,4,5,6,7,8,9}



What if we are dealing with paper like this are dealing? Isolate each digit, rescale, de-slant, ... Hard feature engineering process.

 Target: predicted category or value of the data (column to predict)

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Sepal length	Sepal width	Petal length	Petal width	Species
6.7	3.0	5.2	2.3	Virginica
6.4	2.8	5.6	2.1	Virginica
4.6	3.4	1.4	0.3	Setosa
6.9	3.1	4.9	1.5	Versicolor
4.4	2.9	1.4	0.2	Setosa
4.8	3.0	1.4	0.1	Setosa
5.9	3.0	5.1	1.8	Virginica
5.4	3.9	1.3	0.4	Setosa
4.9	3.0	1.4	0.2	Setosa
5.4	3.4	1.7	0.2	Setosa

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	Species	Petal width	Petal length	Sepal width	Sepal length
	Virginica	2.3	5.2	3.0	6.7
Target	Virginica	2.1	5.6	2.8	6.4
Turget	Setosa	0.3	1.4	3.4	4.6
	Versicolor	1.5	4.9	3.1	6.9
	Setosa	0.2	1.4	2.9	4.4
	Setosa	0.1	1.4	3.0	4.8
	Virginica	1.8	5.1	3.0	5.9
	Setosa	0.4	1.3	3.9	5.4
	Setosa	0.2	1.4	3.0	4.9
	Setosa	0.2	1.7	3.4	5.4

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- Target: predicted category or value of the data (column to predict)
- Features: properties of the data used for prediction (non-target columns)

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Features

Sepal length	Sepal width	Petal length	Petal width	Species
6.7	3.0	5.2	2.3	Virginica
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5.4	3.4	1.7	0.2	Setosa

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- Target: predicted category or value of the data (column to predict)
- Features: properties of the data used for prediction (non-target columns)
- Example: a single data point within the data (one row)

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	Sepal length	Sepal width	Petal length	Petal width	Species
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	6.4	2.8	5.6	2.1	Virginica
Examples 🔶	4.6	3.4	1.4	0.3	Setosa
	6.9	3.1	4.9	1.5	Versicolor
	4.4	2.9	1.4	0.2	Setosa
	4.8	3.0	1.4	0.1	Setosa
	5.9	3.0	5.1	1.8	Virginica
	5.4	3.9	1.3	0.4	Setosa
	4.9	3.0	1.4	0.2	Setosa
	5.4	3.4	1.7	0.2	Setosa

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- Target: predicted category or value of the data (column to predict)
- Features: properties of the data used for prediction (non-target columns)
- Example: a single data point within the data (one row)
- Label: the target value for a single data point

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Sepal length	Sepal width	Petal length	Petal width	Species	
6.7	3.0	5.2	2.3	Virginica	
6.4	2.8	5.6	2.1	Virginica	
4.6	3.4	1.4	0.3	Setosa	🔶 Label
6.9	3.1	4.9	1.5	Versicolor	
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Outline



2 ML Terminologies

3 ML Applications Examples



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WHAT IS CLASSIFICATION?

A flower shop wants to guess a customer's purchase from similarity to most recent purchase.



WHAT IS CLASSIFICATION?

Which flower is a customer most likely to purchase based on similarity to previous purchase?




WHAT IS CLASSIFICATION?

Which flower is a customer most likely to purchase based on similarity to previous purchase?





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WHAT IS CLASSIFICATION?

Which flower is a customer most likely to purchase based on similarity to previous purchase?







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WHAT IS NEEDED FOR CLASSIFICATION?

- Model data with:
 - Features that can be quantitated

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WHAT IS NEEDED FOR CLASSIFICATION?

- Model data with:
 - Features that can be quantitated
 - Labels that are known

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WHAT IS NEEDED FOR CLASSIFICATION?

- Model data with:
 - Features that can be quantitated
 - Labels that are known
- Method to measure similarity

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WHAT IS NEEDED TO SELECT A KNN MODEL?

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WHAT IS NEEDED TO SELECT A KNN MODEL?

- Correct value for 'K'
- How to measure closeness of neighbors?



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K NEAREST NEIGHBORS DECISION BOUNDARY



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K NEAREST NEIGHBORS DECISION BOUNDARY



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VALUE OF 'K' AFFECTS DECISION BOUNDARY



VALUE OF 'K' AFFECTS DECISION BOUNDARY



Methods for determining 'K' will be discussed in next lesson

MEASUREMENT OF DISTANCE IN KNN



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MEASUREMENT OF DISTANCE IN KNN



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EUCLIDEAN DISTANCE



Image: A math a math

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EUCLIDEAN DISTANCE (L2 DISTANCE)



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MANHATTAN DISTANCE (L1 OR CITY BLOCK DISTANCE)



August 28, 2020

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COMPARISON OF FEATURE SCALING METHODS

- Standard Scaler: Mean center data and scale to unit variance
- Minimum-Maximum Scaler: Scale data to fixed range (usually 0–1)
- Maximum Absolute Value Scaler: Scale maximum absolute value

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Import the class containing the scaling method

from sklearn.preprocessing import StandardScaler

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Import the class containing the scaling method

from sklearn.preprocessing import StandardScaler

Create an instance of the class

StdSc = StandardScaler()

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Import the class containing the scaling method

from sklearn.preprocessing import StandardScaler

Create an instance of the class

StdSc = StandardScaler()

Fit the scaling parameters and then transform the data

StdSc = StdSc.fit(X data)

X_scaled = KNN.transform(X_data)

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Import the class containing the scaling method from sklearn.preprocessing import StandardScaler

Create an instance of the class

```
StdSc = StandardScaler()
```

Fit the scaling parameters and then transform the data StdSc = StdSc.fit(X_data) X_scaled = KNN.transform(X_data)

Other scaling methods exist: MinMaxScaler, MaxAbsScaler.

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MULTICLASS KNN DECISION BOUNDARY



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REGRESSION WITH KNN



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CHARACTERISTICS OF A KNN MODEL

- Fast to create model because it simply stores data
- Slow to predict because many distance calculations
- Can require lots of memory if data set is large

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Import the class containing the classification method from sklearn.neighbors import KNeighborsClassifier

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Import the class containing the classification method from sklearn.neighbors import KNeighborsClassifier

Create an instance of the class

KNN = KNeighborsClassifier(n_neighbors=3)

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Import the class containing the classification method from sklearn.neighbors import KNeighborsClassifier

Create an instance of the class

```
KNN = KNeighborsClassifier(n_neighbors=3)
```

Fit the instance on the data and then predict the expected value

```
KNN = KNN.fit(X_data, y_data)
```

```
y_predict = KNN.predict(X_data)
```

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Import the class containing the classification method from sklearn.neighbors import KNeighborsClassifier

Create an instance of the class

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KNN = KNeighborsClassifier(n_neighbors=3)
```

Fit the instance on the data and then predict the expected value

```
KNN = KNN.fit(X_data, y_data)
y predict = KNN.predict(X data)
```

The fit and predict/transform syntax will show up throughout the course.

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Import the class containing the classification method from sklearn.neighbors import KNeighborsClassifier

Create an instance of the class

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KNN = KNeighborsClassifier(n_neighbors=3)
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Fit the instance on the data and then predict the expected value

```
KNN = KNN.fit(X_data, y_data)
```

```
y_predict = KNN.predict(X_data)
```

Regression can be done with KNeighborsRegressor.

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References



https://software.intel.com/content/www/us/en/develop/training

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